

数学冲刺

GMAT



第五章

常见数列及特殊情况处理

本节课授课要点

5.1

常见数列及特殊情况处理

5.1 常见数列及特殊情况处理

递归数列

The sequence $a_1, a_2, a_3, \dots, a_n, \dots$ is such that $a_n = \frac{a_{n-1} + a_{n-2}}{2}$ for all $n \geq 3$, if $a_3 = 4$ and $a_5 = 20$, what is the value of a_6 ?

- A. 12
- B. 16
- C. 20
- D. 24
- E. 28

5.1 常见数列及特殊情况处理

Arithmetic sequence 等差数列

Common difference: 公差

$$a_n = a_1 + (n-1)d \quad \text{通项公式}$$

$$s_n = (a_1 + a_n)n/2 \quad \text{求和公式}$$

$$n = (a_n - a_1)/d + 1$$

5.1 常见数列及特殊情况处理

What is the difference between the sum of all positive even integers less than 102 and the sum of all positive odd integers less than 102 ?

- A. 0
- B. 1
- C. 50
- D. 51
- E. 101

5.1 常见数列及特殊情况处理

Geometric sequence 等比数列

Common ratio: 公比

$$a_n = a_1 q^{n-1}$$

$$S_n = a_1 \cdot \frac{1-q^n}{1-q} \quad (q \neq 0 \text{ 且 } q \neq 1)$$

5.1 常见数列及特殊情况处理

For every integer k from 1 to 10, inclusive, the k th term of a certain sequence is given by $(-1)^{k+1}(\frac{1}{2^k})$. If T is the sum of the first 10 terms in the sequence, then T is

- A. greater than 2
- B. between 1 and 2
- C. between $\frac{1}{2}$ and 1
- D. between $\frac{1}{4}$ and $\frac{1}{2}$
- E. less than $\frac{1}{4}$

5.1 常见数列及特殊情况处理

特殊情况处理

If the sequence $x_1, x_2, x_3, \dots, x_n, \dots$ is such that $x_1 = 3$ and $x_{n+1} = 2x_n - 1$ for $n \geq 1$, then $x_{20} - x_{19} =$

- A. 2^{19}
- B. 2^{20}
- C. 2^{21}
- D. $2^{20} - 1$,
- E. $2^{21} - 1$

回顾本节课授课要点

5.1

常见数列及特殊情况处理

预告下节课授课要点

6.1

排列组合
核心公式与重要思想

6.2

概率公式及排列组合
在概率中的应用

THANK YOU