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# Chapter 1 Arithmetic Kooleon

#### **Objectives:**

- A. 掌握基本算数运算及概念
- B. 了解常见运算涉及的数学术语及题型
- C. 掌握基本的做题套路(百分数增减,比例表达)和速度提升方法

1.1 Integers 整数

#### 1.1.1 Key terms' definition

基本运算: add/ plus 加→sum 和 subtract/minus 减  $\rightarrow$  difference 差 multiply/ time 乘 →product 积 divide 𝔅 → quotient 𝔅 divided by divisible 可被整除的 divisible by remainder 余数 integer 整数 positive number 正数 negative number 负数 factor=divisor 因数 multiple 倍数 least common multiple 最小公倍数 greatest common divisor/ greatest common factor 最大公因数 odd integer 奇数 even integer 偶数 prime number 质数 prime factor / divisor 质因数 composite number 合数 digit 数位 consecutive number 连续数



#### 1.1.2 Strategies

round to the nearest 四舍五入

余数需要注意: 80 divided by 100 is 0 remainder 80.

除法的表达: The result of 19 divided by 7 is the quotient 2 with remainder 5, or simply "2 remainder 5.



乘法的表达: 2/3 as many A as B → 表示 A=2/3\*B twice as many A as B表示 A=2\*B

**The least common multiple:** 两个非零整数a和b的最小公倍数是a和b共同倍数中最小的正整数。例如30和75 的最小公倍数是150.

**The greatest common divisor** (or **greatest common factor**):两个非零整数a和b的最大公因数是a和b共同因数中最大的正整数,例如30和75的最大公因数是15.

**prime number:** 质数是所有大于1的整数中,只有1和它自己两个因数的整数。前十个质数是2,3,5,7,11,13,17,19,23,和29.

prime factor/prime divisor: 质因数是一个数的因数中属于质数的数。下图为分解质因数的例子。

 $12 = (2)(2)(3) = (2^{2})(3)$  14 = (2)(7)  $81 = (3)(3)(3)(3) = 3^{4}$   $338 = (2)(13)(13) = (2)(13^{2})$   $800 = (2)(2)(2)(2)(2)(5)(5) = (2^{5})(5^{2})$ 1,155 = (3)(5)(7)(11)

#### 1.1.3 Exercise

1) If 7.36 is rounded to the nearest tenth and the rounded number is multiplied by 3, what is the result? A. 21.0

- B. 21.9
- C. 22.0
- D. 22.1 E. 22.2

answer: 7.36 被四舍五入到十分位是 7.4, 随后用得到的结果 7.4 乘以三, 答案是 22.2, 选择 E。

2) What number exceeds 50 percent of itself by 10? A. 5 B. 10 C. 15 D. 20 E. 60 answer: D, 注意 exceed by 表达超过的幅度。

#### 1.2 Fractions& Decimals 分数&小数

#### 1.2.1 Key terms' definition

fraction 分数





numerator 分子 denominator 分母 common denominator 公分母 reciprocal 倒数 mixed number 带分数 improper fraction 假分数 decimal 小数 units digit / ones digit 个位 tens digit 十位 hundreds digit 百位 thousands digit 千位 tenths digit 十分位 hundredths digit 百分位 thousandths digit 千分位 rational numbers 有理数

1.2.2 Strategies

irrational number 无理数



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rational numbers: 有理数指所有可以表示为分数式的数字。

**terminate or repeat decimal**: 所有会终止或者循环的小数,都可以是有理数;如果一个小数既不终止 (**terminate**)也不循环(**repeat**),那么它是一个无理数(**irrational number**).

1.3 Exponents and Roots 指数及根

1.3.1 Key terms' definition

base 底数 exponent 指数 power 次方 square 平方 square root 平方根 cube root 立方根 fourth root 四次方根

#### 1.3.2 Strategies

**power** 次方:  $2^5$ =the fifth power of 2.

**root:** 不同次根的表达是需要掌握的重点之一。比如 square root 平方根, cube root 立方根, 以及上升到 4 次以上的表达为序数词+root, 例如 fourth root.



对于奇数次的根(odd-order roots),每一个数字 n 来说都有且仅有一个根,不论 n 是正数还是负数;

对于偶数次的根(even-order roots),每一个正数有且仅有两个根,每一个负数没有根。

例如: 8 有且仅有一个立方根 2, 但是有两个四次方根; -8 有且仅有一个立方根-2, 但是因为是负数, 它 没有四次方根。

1.4 Real Numbers 实数

#### 1.4.1 Key terms' definition

real number 实数 real number line 实数轴 less than 小于 greater than or equal to 大于等于 absolute value 绝对值 interval 区间 inclusive 包含的

1.4.2 Strategies

triangle inequality:  $|a+b| \le |a|+|b|$ 

interval:不等式中包含的所有取值组成的集合。

常见的表达中,需要掌握大于等于(more than or equal to),小于等于(less than or equal to).

1.5 Ratio& Percent 比例/百分比

## 1.5.1 Key terms' definition

ratio 比例 proportion 比例式 percent 百分比 percent change 百分比变化 percent increase/decrease 百分比增/减

#### 1.5.2 Strategies

**percent change:** 运算中最重要的是记得百分比变化计算式的分母一定是**原始数值(original value).**例如, 100 下降到 80 的 percent change 计算方法是(100-80)/100=20%。



increase by x percent / decrease by x percent: 增长/降低了百分之 x.

#### 1.5.3 Exercise

The population of Country X for 1980 was p. The population of Country X increased by 3.8 percent in each of the next two years.

Quantity A: The population of Country X for 1982. Quantity B: 1.076p

- A. Quantity A is greater.
- B. Quantity B is greater.
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given.

answer: A

1.6 New Definition Problem 新定义题

#### **1.6.1 Strategies**

- 1. 分析定义-长难句
- 2. 看懂例子
- 3. 套用条件



1) An integer k is a "half square" if 2k is the square of a positive integer. For example, 18 is a half square because  $2X18=36=6^2$ . What is the smallest half square that is greater than 100?

answer: 本题新定义为"half square",注意学生不应纠结翻译字面,而是理解实际的定义含义,即一个数如 果两倍是一个平方数,那么该数就是一个"半平方数",要求大于100的最小的半平方数,应寻找大于200的 最小的平方数,但225除以二无法得到整数,所以应该是第二小的平方数256的一半,答案为128.

2) A number is a palindrome if it can be written the same backwards and forwards (6336 is an example of a palindrome). What number divides into every 4 digit palindrome?

A. 2

B. 3

C. 7

D. 11

answer:本题的新定义是palindrome回文数字,即从左往右和从右往左一样的数字,问句问哪个数字一定可以整除回文数字,可以用xyyx来表示回文数字,则其实际大小为1000x+100y+10y+x=1001x+110y,明显可被11整除。答案为D

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#### Mixed Practice 1

1. Which of the integers 2, 9, 19, 29, 30, 37, 45, 49, 51, 83, 90, and 91 are prime numbers?

- 2. A particular stock is valued at \$40 per share. If the value increases by 20 percent and then decreases by 25 percent, what will be the value of the stock per share after the decrease?
- 3. When the positive integer *n* is divided by 3, the remainder is 2 and when *n* is divided by 5, the remainder is 1. What is the least possible value of *n* ?

#### Answers:

- 1. 2, 19, 29, 37 and 83
- 2. \$36 per share

3.11

#### **Mixed Practice 2**

1. *n* is an integer.

Quantity A:  $(-1)^{n}(-1)^{n+2}$ Quantity B:1

- A. Quantity Ais greater.
- B. Quantity B is greater.
- C. The two quantities are equal
- D. The relationship cannot be determined from the information given.
- 2. x is an integer greater than 3.

Quantity A: The number of even factors of 2xQuantity B: The number of odd factors of 3x

- A. Quantity Ais greater.
- B. Quantity B is greater.
- C. The two quantities are equal
- D. The relationship cannot be determined from the information given.

## 3. What is the remainder when $3^{283}$ is divided by 5?

- A. 0
- **B**. 1
- C. 2
- D. 3
- E. 4
- 4. If x < y, which of the following must be true?



- D. 2x y < y
- E. 2x-y < 2xy
- 5. If n and m are positive integers and m is a factor of  $2^6$ , what is the greatest possible number of integers that can be equal to both 3n and  $2^6/m$  ?
  - A. Zero
  - B. One
  - C. Three
  - D. Four
  - E. Six
- 6. Amy and Jed are among the 35 people, who are standing in a line, one behind the other, waiting to buy movie tickets. The number of people in front of Amy plus the number of people behind Jed is 24. If there are 15 people behind Amy, including Jed, how many people are in front of Jed?
  - A. 23
  - B. 25
  - C. 27
  - D. 29
  - E. 31
- 7. The discounted price of a certain suit is 20 percent less than the original price of the suit. If the discounted price of the suit plus a sales tax of 5 percent of the discounted price equals \$67.20, what was the original price of the suit?
  - A. \$70.50
  - B. \$73.90
  - C. \$76.00
  - D. \$79.80
  - E. \$80.00
- 8. Greg's weekly salary is \$187, which is 15 percent less than Karla's weekly salary. If Karla's weekly salary increases by 10 percent, by what percent must Greg's weekly salary increase in order to equal Karla's new weekly salary?

Give your answer to the nearest tenth of a percent.

9. xy>o

Quantity A:  $x^4y^3$ 

Quantity B: 0

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given
- 10. Which of the following pairs of integers have reciprocals whose sum is either less than 1/3 or greater than 1/2?

Indicate all such pairs.

- $\Box$  1 and 14
- $\square \ 3 \ and \ 12$
- $\square\ 5 \ and\ 10$
- $\Box$  7 and 8
- 11. In 1988 Mr. Smith's annual income was greater than Mrs. Smith's annual income. In 1989 Mr. Smith's annual income decreased by *p* percent. Whereas Mrs. Smith's annual income increased by *p* percent. *p*>0 Quantity A: Mr. and Mrs. Smith's combined annual income in 1988 Quantity B: Mr. and Mrs. Smith's combined annual income in 1989



- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given
- 12. The original value of machine X is V dollars, while the original value of machine Y is 2V dollars. Both machines depreciate in value at a constant rate of 10 percent of their original value per year. Quantity A: The value of machine X after 3 years Quantity B: The value of machine Y after 6 years
  - A. Quantity A is greater
  - B. Quantity B is greater
  - C. The two quantities are equal.
  - D. The relationship cannot be determined from the information given
- 13. A number is considered "odd-mult" if it is the product of exactly two consecutive odd numbers. How many positive numbers less than 400 are "odd-mult"?

14. The 20 people at a party are divided into n mutually exclusive groups in such a way that the number of people in any group does not exceed the number in any other group by more than 1.Quantity A: The value of n if at least one of the groups consists of 3 people Quantity B: 6

A. Quantity A is greater

- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given
- $15. \ \ If \ n \ is \ a \ positive \ integer \,, \quad then \ n^+ \ denotes \ a \ number \ such \ that \ n < n^+ < n \ + 1.$

Quantity A:  $20^+/4^+$ Quantity B:  $5^+$ 

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given
- 16. Both P and Q are positive numbers, and S is a negative number. Which of the following fractions could be undefined?
  - A. P/Q+S
  - B. Q/P+S
  - C. S/P+Q
  - D. Q/S-P
  - E. S/P-Q
- 17. For a certain event, 148 people attended. If all 148 had paid full admission price, the total revenue would be three times the cost of sponsoring the event. (Admission price was the only source of revenue.) As it happens, only 50 paid the full admission price, and the others paid nothing.

Quantity A: the total revenue

Quantity B: the cost of sponsoring the event

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given





А А В В

 $\frac{\times B}{C B 5 B}$ 

. If A,B and C represent different digits in the multiplication, then A+B+C=

- A. 9
- B. 12
- C. 14
- D. 15
- E. 17

19.

Quantity A: The number of distinct prime factors of  $20^6$ Quantity B: The number of distinct prime factors of  $32^{10}$ 

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given

20. n is a positive integer, and k is the product of all integers from 1 to n inclusive. If k is a multiple of 1440, then the smallest possible value of n is\_\_\_\_\_

- A. 8
- B. 12
- C. 16
- D. 18
- E. 24
- 21. M is a positive two-digit number. When the digits are reversed, the number is N. If K = M + N, which of the following is true?
  - A. K must be even
  - B. K cannot be square
  - C. K cannot be divisible by 13
  - D. K must be divisible by 11
  - E. If M is even then K must be even

22. If  $n = 2 \times 3 \times 5 \times 7 \times 11 \times 13 \times 17$ , then which of the following statements must be true?

- I.  $n^2$  is divisible by 600
- II. n + 19 is divisible by 19
  - n+4
  - $\frac{n+1}{2}$
- III. 2 is even
- A. I only
- B. II only
- C. III only
- D. I and III
- E. None of the above

23. How many integers from 1 to 900 inclusive have exactly 3 positive divisors?

- A. 10
- **B.** 14
- C. 15
- D. 29
- E. 30













**Answers and Explanations** 

- 1. C
- 2. D
- 3. C
- 4. D 5. A
- 6. 注意站队时的前后人数是不包括May和Jed的。
- 7. E 本题虽然有plus 但是消费税率应该是乘以打折后的价格才是消费税
- 8. 29.4,本题先计算Karla的薪金,再用其1.1倍除以187得到倍数。需要注意percent less, increase by的数学 含义,by表达增减幅度
- 9. xy 大于 0 有可能都为正数,也有可能都为负数,前一种情况 A 大于 B,后一种则反之。
- 10. ACD
- 11. A
- 12. B
- 13. 最接近 400 的是 19X21=399,因为是连续数字,从 1X3 开始总共 10 对
- 14. 本题需要理解题干的分组要求,每一组的人数之间差值不得大于 1。Quantity A 中若有一组人数为 3, 其他组人数要么都为 3 但不可能,要么有 2 人组;要么有 4 人组。分情况讨论 2 人+3 人组,则最多有 9 组,最少 7 组,都大于 Quantity B;讨论 2 人+4 人组,则可以有 6 组-4 人组 4 个,2 人组 2 个,等于 Quantity B,所以答案无法判断。
- 15. 20<sup>+</sup> 和 4<sup>+</sup>各自的大小不定,其比值也会是不定的,Quantity B 也是不定值,其关系无法判断。
- 16. ABE. 数学术语 undefined 意为不可定义,分数不可定义的情况是分母为 0,正负数相加可能为 0,正数 相减也可能为 0.
- 17. A
- 18. E. 题中的 B 可以是 1, 5, 6。 B=1 可以直接排除,将 5 代入发现无论 A 取何值,积的十位数都不为 5,排除;将 6 代入后,发现要使积的十位数为 5,则 A 可以取 2 or 7;将 2 代入后发现积的百位不为 6,排除;将 7 代入后发现都满足,且得出 C 为 4;所以 6+7+4=17.
- 19. A. 注意 distinct prime factor 是不同的质因数,也就是重复的都不算。则 20 只有 2 和 5,6 次方后有 12 个质因数;32 只有一个 2 是质因数,10 次方则有 10 个质因数。
- 20. A
- 21. D
- 22. E 23. A **KOO** E





2.1 Operations with Algebraic Expression 代数表达式的运算

2.1.1 objectives

A.代数表达式的定义 B.代数表达式的加减乘除运算

2.1.2 Key terms' definition

equation 等式,方程 linear equation 线性方程 quadratic equation 二次方程 algebraic term 代数项 like terms / similar terms 同类项 variable 变量 numerical coefficient 数字系数 literal coefficient 字母系数 constant 常数 identity 恒等式



2.1.3 Strategies

identity: 恒等式, e.g.

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 $(a + b)^{2} = a^{2} + 2ab + b^{2}$   $(a - b)^{3} = a^{3} - 3a^{2}b + 3ab^{2} - b^{3}$   $a^{2} - b^{2} = (a + b)(a - b)$ (代数式运算的三大基本形式: 3x + 5 = -2 A linear equation in one variable, x x - 3y = 10 A linear equation in two variables, x and y  $20y^{2} + 6y - 17 = 0$  A quadratic equation in one variable, y



2.2 Rules of Exponents 指数运算法则

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2.2.1 objectives

A.记忆指数运算的七大法则 B.熟练运用七大法则

#### 2.2.2 Key terms' definition

base 底 exponent 指数

#### 2.2.3 Strategies



$$x^{b} = x^{a}$$

$$x^{b-a}$$

$$x^{b-a}$$

$$x^{0} = 1$$

$$(x^{a})(y^{a}) = (xy)^{a}$$

$$(x^{a})^{a} = \frac{x^{a}}{y^{a}}$$

$$(x^{a})^{b} = x^{ab}$$

#### 2.2.4 Exercises 练习题

1. n is an integer.

Quantity A:  $(-1)^{n}(-1)^{n+2}$ Quantity B: 1

- E. Quantity A is greater
- F. Quantity B is greater
- G. The two quantities are equal.
- H. The relationship cannot be determined from the information given

answer:根据公式第二条 Quantity A:负1的指数为2(n+1),为偶数,那么负数的偶数次幂为正数,



所以 Quantity A 与 Quantity B 相等都为一,选C。

2.3 Solving Linear Equation 线性方程

2.3.1 objectives

A.线性方程及方程组的求解

#### 2.3.2 Key terms' definition

equivalent equations 等价方程式 a system of equations 方程组 simultaneous equations 联立方程

#### 2.3.3 Strategies





equivalent equations: 拥有相同解的方程 substitution: 连立法 elimination: 消元法

### 2.4 Solving Quadratic Equations 二次方程求解



A. 熟练使用求根公式

#### 2.4.2 Key terms' definition

Quadratic Equations 二次方程

#### 2.4.3 Strategies

一元二次方程形如:

 $ax^2 + bx + c = 0$ 

quadratic formula 求根公式:



# $f_{x} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

除了求根公式之外,还有一种方法,十字交叉/因式分解法 (factoring):

 $5x^{2} + 3x - 2 = 0$ (5x - 2)(x + 1) = 0

#### 2.5 Solving Linear Inequalities 解一次不等式

#### 2.5.1 objectives

A.掌握一次不等式求解

#### 2.5.2 Key terms' definition

Inequalities 不等式 solution set 解集





#### 2.5.3 Strategies 主要知识点

- < less than
- > greater than
- ≤ less than or equal to
- ≥ greater than or equal to

不等式两边同时乘/除以负数时需要反号.

2.6 Functions 函数

2.6.1 objectives

A.理解函数定义

#### 2.6.2 Key terms' definition

function 函数



range 值域 domain 定义域

#### 2.6.3 Strategies 主要知识点

函数一般形如: f(x) = 3x+5

2.7 Applications 函数应用

#### 2.7.1 Key terms' definition

interest 利息 rate 率 interest rate 利率 principal 资本 profit 利润 margin 利润 single interest 单利 compound interest 复利 discount 折扣 original price 原价 list price 标价 sale price 卖价 purchasing price 买价 retail value 零售价 tax 税 mark up 涨价 mark down 降价



#### 2.7.2 Strategies 主要知识点

Simple interest 单利模式: Simple interest is based only on the initial deposit, which serves as the amount on which interest is computed, called the principal, for the entire time period. If the amount P is invested at a simple annual interest rate of r percent, then the value V of the investment at the end of t years is given by the formula:

$$V = P\left(1 + \frac{rt}{100}\right)$$

compound interest 复利模式: In the case of compound interest, interest is added to the principal at regular time intervals, such as annually, quarterly, and monthly. Each time interest is added to the principal, the interest is said to be compounded. After each compounding, interest is earned on the new principal, which is the sum of the preceding principal and the interest just added. If the amount P is invested at an annual interest rate of r percent, compounded annually, then the value V of the investment at the end of t years is given by the formula:



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$$t = P\left(1 + \frac{r}{100}\right)^{t}$$

If the amount P is invested at an annual interest rate of r percent, compounded n times per year, then the value V of the investment at the end of t years is given by the formula:

$$V = P \left( 1 + \frac{r}{100n} \right)^{nt}$$

#### 2.7.3 Exercise 练习

1. A mixture of 12 ounces of vinegar and oil is 40 percent vinegar, where all of the measurements are by weight. How many ounces of oil must be added to the mixture to produce a new mixture that is only 25 percent vinegar?

answer: 7.2

2. If an amount P is to be invested at an annual interest rate of 3.5 percent, compounded annually, what should be the value of P so that the value of the investment is \$1,000 at the end of 3 years?

answer: 901.94



2.8 Coordinate Geometry 坐标几何

2.8.1 objectives

A. 理解定义

B. 熟悉利用图像解线性不等式方程组(线性规划)

2.8.2 Key terms' definition

coordinate system 坐标系 rectangular coordinate system 直角坐标系 xy-coordinate system / xy-plane 平面直角坐标系 origin 原点 x-axis x 轴 y-axis y 轴 x-coordinate / abscissa 横坐标 y-coordinate / ordinate 纵坐标 number line 数轴 quadrant 象限 slope 斜率 intercept 截距 symmetric 对称



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#### 2.8.3 Strategies 主要知识点





• *P*' is the reflection of *P* about the *x*-axis, or *P*' and *P* are symmetric about the *x*-axis.

• *P*" is the reflection of *P* about the *y*-axis, or *P*" and *P* are symmetric about the *y*-axis.

• *P*<sup>\*\*</sup> is the reflection of *P* about the origin, or *P*<sup>\*\*</sup> and *P* are symmetric about the origin



#### 2.8.4Exercises 练习题

Example 2.8.3: Consider the following system of linear inequalities.

$$\begin{array}{l} x - 3y \ge -6\\ 2x + y \ge -1 \end{array}$$





#### 2.9 Graphs of Functions 函数图像





2.9.1 objectives

- A. 熟悉各类函数图像特征
- B. 熟悉图像的变化和位移与各系数变化的对应关系

2.9.2 Key terms' definition

parabola 抛物线 vertex 顶点 vertices 顶点(复数) line of symmetry 对称轴 piecewise-defined function 分段函数

#### 2.9.3 Strategies 主要知识点

二次函数 y = ax2 + bx + c
 a 的正负决定开口方向(a>0开口向上,a<0开口向下).c 为 y 轴截距.</li>
 line of symmetry 对称轴:

$$x = -\frac{b}{2a}$$

vertex 顶点:

$$\left(-\frac{b}{2a},\frac{4ac-b^2}{4a}\right)$$





2. 圆的方程: (x-a)2+(y-b)2=r2





### 例如绝对值函数:

$$\begin{split} h(x) &= |x| \\ \to \ h(x) &= \begin{cases} -x, \ x < 0 \\ x, \ x \geq 0 \end{cases} \end{split}$$



4. **幂函数** f(x) = xa

a>0 时,图像经过点(1,1)和(0,0).

函数的图像在区间[0,+∞)上是增函数.

当 α<0 时,图像都通过点(1,1).

b、图像在区间(0,+∞)上是减函数.





#### 5. 函数图像的位移

In general, for any function h(x) and any positive number c, the following are true.

- The graph of h(x) + c is the graph of h(x) shifted upward by c units.
- The graph of h(x) c is the graph of h(x) shifted downward by c units.
- The graph of h(x + c) is the graph of h(x) shifted to the left by c units.
- The graph of h(x c) is the graph of h(x) shifted to the right by c units.
- The graph of ch(x) is the graph of h(x) stretched vertically by a factor of c if c > 1.
- The graph of ch(x) is the graph of h(x) shrunk vertically by a factor of c if 0 < c < 1.

Mixed Practice 1.



For each of the following functions, give the domain and a description of the graph y = f(x) in

the xy-plane, including its shape, and the x- and y-intercepts.

(a) 
$$f(x) = -4$$

- (b) f(x) = 100 900x
- (c)  $f(x) = 5 (x + 20)^2$
- (d)  $f(x) = \sqrt{x+2}$

(e) 
$$f(x) = x + |x|$$

2.

In the coordinate system below, find the following.

- (a) Coordinates of point Q
- (b) Lengths of PQ, QR, and PR
- (c) Perimeter of  $\triangle PQR$
- (d) Area of  $\triangle PQR$
- (e) Slope, y-intercept, and equation of the line passing through points P and R



3.

Pat invested a total of \$3,000. Part of the money was invested in a money market account that paid 10 percent simple annual interest, and the remainder of the money was invested in a fund that paid 8 percent simple annual interest. If the interest earned at the end of the first year from these investments was \$256, how much did Pat invest at 10 percent and how much at 8 percent?

4.

Two cars started from the same point and traveled on a straight course in opposite directions for exactly 2 hours, at which time they were 208 miles apart. If one car traveled, on average, 8 miles per hour faster than the other car, what was the average speed of each car for the 2-hour trip?



Answers:

- 1.
- (a) Domain: the set of all real numbers. The graph is a horizontal line with y-intercept -4 and no x-intercept.
- (b) Domain: the set of all real numbers. The graph is a line with slope -900, y-intercept 100, and x-intercept <sup>1</sup>/<sub>9</sub>.
- (c) Domain: the set of all real numbers. The graph is a parabola opening downward with vertex at (-20, 5), line of symmetry x = -20, y-intercept -395, and x-intercepts  $-20 \pm \sqrt{5}$ .
- (d) Domain: the set of numbers greater than or equal to -2. The graph is half a parabola opening to the right with vertex at (-2, 0), x-intercept -2, and y-intercept  $\sqrt{2}$ .
- (e) Domain: the set of all real numbers. The graph is two half-lines joined at the origin: one half-line is the negative x-axis and the other is a line starting at the origin with slope 2. Every nonpositive number is an x-intercept, and the y-intercept is 0. The function is equal to the following piecewise-defined function

$$f(x) = \begin{cases} 2x, & x \ge 0\\ 0, & x < 0 \end{cases}$$

2.

- (a) (-2, 0)
- (b) PQ = 6, QR = 7,  $PR = \sqrt{85}$
- (c)  $13 + \sqrt{85}$
- (d) 21
- (e) Slope:  $-\frac{6}{7}$ ; *y*-intercept:  $\frac{30}{7}$ ; equation of line:  $y = -\frac{6}{7}x + \frac{30}{7}$ , or 7y + 6x = 30
- 3. \$800 at 10% and \$2,200 at 8%
- 4. 48 mph and 56 mph





Chapter 3 Geometry KOOleon 新有巧在名

### **Objectives:**

- A. 了解平面几何中线、角、三角形、四边形和多边形的性质,能够转化边角关系, 熟练计算各类特殊 三角形中的边、角问题等。理解各类混合图形中的测算问题,并通过平面几何的计算能够解决实际生 活中遇到的问题。
- B. 熟悉圆的各项性质: 半径、直径、弧长、圆心角和圆周角等内容, 熟练计算圆的周长面积。
- C. 培养立体几何的空间概念, 能够借助辅助线将三维图形转化成平面几何中的三角形、四边形或者圆 来计算, 能够运用简单的立体几何中表面积和体积等概念去解决实际生活中的现实问题。

#### 3.1 Lines and Angles

#### 3.1.1. Objective:

- 1. 理解线、线段、中点, 端点等基础概念
- 2. 了解各种类型的角,特别在两线平行时各类角的相互关系。
- 3. 能够结合特殊三角形、正方形、长方形和圆等图形,熟悉特定角度和边长的转化关系。

#### 3.1.2. Key terms' definition



angle 角 degree 角度 intersect 相交 opposite angles / vertical angles 对顶角 (∠AOD and ∠BOC) congruent angles 等角: angles that have equal degrees







Figure not drawn to scale 图形不按比例绘制

#### 3.1.3. Exercises

1. In the diagram, AE = 20, AD = 14, CD = 6 and EB = 17. What is the length of line segment BC? Note: Figure not drawn to scale. A.2 B.3 C.4 D.5 E.6 Answer: D

#### **3.2 Polygons**

#### 3.2.1. Objective:

A. 掌握多边形的内角和计算公式,了解多边形的内角、对角线、边长和面积的计算方法。





3.2.2. Key terms' definition

polygon 多边形 side 边 vertex 交点 vertices 交点 (复数) triangle 三角形 quadrilateral 四边形 pentagon 五边形 hexagon 六边形 octagon 八边形 decagon 十边形 regular polygon 正多边形 perimeter 周长 area 面积

#### 3.2.3. Strategies

n 边形的内角和公式 = (n-2) ×180°, 例如: 六边形的内角和= (6-2) ×180° =720°

n边形内联结任意不相邻的三个顶点可以形成图内三角形,图内三角形的总个数=n-2





多边形考点比较简单集中:内角和公式一定要熟练应用,只有正多边形能计算出单个内角和的值。其余情况可以参考连接对角线,转化成三角形计算。

多边形的面积计算基本转化成多个三角形的叠加计算。

#### 3.2.4. Exercises

1. The figure shows a regular 9-sided polygon. What is the value of x ?







2. Polygon SUVNPQ is equilateral and equiangular and TWOR is a rectangle.



- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given



#### **3.3 Triangles**

#### 3.3.1. Objective:

A. 了解三角形的边长和角的关系,能够在三角形内做出辅助线化解一般三角形或者多边形中的复杂问题, 掌握周长和面积的计算方法。

B. 重点掌握直角三角形、等腰三角形和正三角形的计算问题,包括:边长、角度、周长和面积等。

C. 对于特殊直角三星的边长比例和角度关系要能够熟练进行转换,能够将复杂图形内的问题化简回归 到同一三角形内解决。

#### 3.3.2. Key terms' definition

right triangles 直角三角形 hypotenuse 斜边 leg 直角边



Pythagorean theorem 勾股定理 equilateral triangle 等边三角形 isosceles triangle 等腰三角形

base 底 height 高

congruent triangle 全等三角形 similar triangles 相似三角形

#### 3.3.3 Strategies

1. 请熟记常见直角三角形的边长关系, 最常考到的边长比为 3:4:5 或 6:8:10 或 5:12:13.

2. 熟记特殊三角形的角度与边长关系:

 $30^{\circ}$  :  $60^{\circ}$  :  $90^{\circ}$  - 1: $\sqrt{3}$ : 2

45° : 45° : 90° - 1:1:√2

 $60^{\circ}$  :  $60^{\circ}$  :  $60^{\circ}$  - 1:1:1

3. 三角形的面积公式 S=底边×高÷2, 三角形的任一边都可以成为底边, 高则是垂直于底边的线段(起于 对应顶点, 终于底边)。

4. 全等三角形 (congruent triangle): 两个三角形的三条边和三个角完全一致。只要满足下列任一条件, 即可判断两个三角形为全等三角形。

边边边(Side-Side-Side):三边对应相等的三角形是全等三角形。

• 边角边 (Side-Angle-Side): 两边及其夹角对应相等的三角形是全等三角形。

角边角(Angle-Side-Angle):两角及其夹边对应相等的三角形全等。

5. 相似三角形(similar triangles):如果一个三角形的两条边和另一个三角形的两条边对应成比例,并且对 应的夹角相等,那么这两个三角形相似。对应相似边的比例相同,面积比为边长比的平方。



Since triangles *ABC* and *DEF* are similar, we have  $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$ . By cross multiplication, we can obtain other proportions, such as  $\frac{AB}{BC} = \frac{DE}{EF}$ .

6. 一旦涉及到三角形的比较大小题目,除非标明 drawn to scale,大多数题目的图形不按比例绘制,不可 根据图形解题。 实际考试中推荐自己绘图,适当考虑添加辅助线。

7. 三角形两边之和大于第三边,两边之差小于第三边.



- A. Quantity A is greater
- B. Quantity B is greaterC. The two quantities are equal.
- D. The relationship cannot be determined from the information given

Answer: D

2. If x > 0, and two sides of a certain triangle have lengths 2x+1 and 3x+4 respectively, which of the following could be the length of the third side of the triangle?

- A. 4x + 5B. x + 2C. 6x + 1
- D. 5x+6
- E. 2x + 17

Answer: A C E

#### 3. What are the lengths of sides NO and OP in triangle NOP below?



Answer: NO= 30 and OP=  $10\sqrt{34}$ 

4. In the figure below, If the area of triangle AB = BC = CD. CDE is 42, what is the area of triangle ADG?





The length of AB is  $10\sqrt{3}$ .

Which of the following statements individually provide(s) sufficient additional information to determine the area of triangle ABC above?

Indicate all such statements.

- A . DBC is an equilateral triangle.
- B. ABD is an isosceles triangle.
- C . The length of BC is equal to the length of AD.
- D. The length of BC is 10.
- E. The length of AD is 10.

Answer: A, D

6.





Quantity A

180+a

b+c

Quantity A

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given

Answer: C

#### **3.4 Quadrilaterals**

#### 3.4.1. Objective

- A. 了解四边形的概念 , 能够转化各类四边形成为以单个三角形为单位的运算。
- B. 熟练掌握正方形、长方形、梯形的周长面积运算。
- C. 理解平行四边形(包括正方形、长方形、菱形)的角、对角线、边长的特定性质。



3.4.2. Definition of key terms

rectangle 长方形 length 长 width 宽 square 正方形 side 边,边长 parallelogram 平行四边形 trapezoid 梯形 rhomb 菱形 bisector 平分线 diagonal 对角线

#### 3.4.3. Strategies

- 1. 平行四边形的重点复习正方形和长方形的对角线计算,例如:正方形的两条对角线相互垂直。
- 2. 平行四边形计算角度的问题一般先转化成单个三角形, 然后利用三角形的内角和来进行计算。

2			
3.	半行四辺形面积 S=base × hei	nt, 梯形面积 $S=\frac{1}{2}(base_1+base_2) \times height$	

#### 3.4.4. Exercises



 $A \xrightarrow{B} \xrightarrow{-2} \xrightarrow{-$ 

```
Answer: \sqrt{29}
```

2.



The figure above represents a rectangular garden with a walkway around it. The garden is 18 feet long and 12 feet wide. The walkway is uniformly 3 feet wide, and its edges meet at right angles. What is the area of the walkway?



Answer: 216 square feet.

3. A, B, and C are three rectangles. The length and width of rectangle A are 10 percent greater and 10 percent less, respectively, than the length and width of rectangle C. The length and width of rectangle B are 20 percent greater and 20 percent less, respectively, than the length and width of rectangle C.

Quantity A :The area of rectangle A Quantity B:The area of rectangle B

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given

Answer: A

3.5 Circles

3.5.1. Objective:

- A. 了解圆的基本性质: 半径、直径、周长和面积的计算。这也包括各类圆与其他图形的结合题。
- B. 掌握圆心角、圆周角的运算方法, 能够计算对应弧长。
- C. 灵活应对各类圆形的复杂图形:同心圆,扇形等的周长面积等运算。
- D. 了解相切的定义, 能够运算内切和外切的圆类题目。
- E. 熟练掌握圆内接三角形的性质,能够有效转换边长和半径、直径的长度关系,充分利用三角形的知识 解决复杂的图形问题 。

#### 3.5.2. Definition of key terms

circle 员 center 圆心DF.CN radius 半径 radii 半径 (复数) diameter 直径 chord 弦 circumference 圆的周长 arc 弧 radian 弧度 central angle 圆心角 semicircle 半圆 sector 扇形 tangent 相切 tangent line 切线 point of tangency 切点 intersect 相交 inscribe 内接 / 内切 circumscribe 外接 / 外切 internally tangent 内切

externally tangent 外切


concentric circles 同心圆

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#### 3.5.3. Strategies

1. chord 弦: 连接圆上任意两点的线段叫做弦,经过圆心的弦叫做直径,直径是一个圆里最长的弦。例如: 图中的 PQ, ST 都是弦。



2. 圆的周长 (circumference) 公式 C=2Πr=Πd, 面积公式 S=Πr<sup>2</sup>, Π≅ 3.14。

3. 弧 (arc): 圆上任意两点间的部分叫做圆弧,简称弧。圆弧的度数可以直接用圆心角表达,例如:弧 ABC 的度数为 50°,圆弧 ADC 的度数为 310°。圆弧的弧长通过弧度与圆周角 (2π)的比例来计算,例如 弧 ABC 的长度=  $50\%360° \times 2\pi \times 5\approx 4.4$ 。



4. A polygon is inscribed in a circle if all its vertices lie on the circle, or equivalently, the circle is circumscribed about the polygon.



A polygon is circumscribed about a circle if each side of the polygon is tangent to the circle, or equivalently, the circle is inscribed in the polygon. In the figure below, quadrilateral ABCD is circumscribed about the circle with center O.



5. 相切(tangent): 一条直线和一个圆有且仅有一个交点的时候,该圆与直线相交。这条直线为切线(tangent line),该交点为切点(point of tangency,例如: P 点)。连接圆心和切点的线段比为半径,且
垂直于切线;反之亦然.





6. 当圆内接三角形有一边是直径的时候,该边对应的角为直角;反之,当圆内接三角形有一个角为直角 时,该三角形必有一边为直径。



#### 3.5.4. Exercises

1 . The area of a circle is equal to the area of a square. Quantity A

The circumference of the circle.

<u>Quantity B</u> The perimeter of the square.

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given

#### Answer: B

2.



The circle with center O above has radius = 4. Find the following.

- (a) Circumference of the circle
- (b) Length of arc ABC
- (c) Area of the shaded region

Answer: (a)  $8\pi$  (b)  $\frac{8\pi}{9}$  (c)  $\frac{16\pi}{9}$ 

koolearn

3.

The figure below shows two concentric circles, each with center O. Given that the larger circle has radius 12 and the smaller circle has radius 7, find the following.





4.



O is the center of the circle above.

Quantity A: x Quantity B: 5

- A. Quantity A is greater
- B. Quantity B is greater
- C. The two quantities are equal.
- D. The relationship cannot be determined from the information given

Answer: B

5.



AB is the diameter of the circle. If AF=BF= $3\sqrt{2}$  and AC=5, what is the area of square BCDE?

Answer: 11

6.



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O is the center of the semicircle. If  $\angle BCO = 30$  and  $BC = 6\sqrt{3}$ , what is the area of  $\triangle ABO$ ?

- B.  $6\sqrt{3}$
- C.  $9\sqrt{3}$
- D.  $12\sqrt{3}$
- E.  $12\sqrt{3}$

Answer: C



#### 3.6.1. Objective:

A. 了解立方体的基本概念,周长、表面积和体积的计算公式。

- B. 重点掌握立方体、正方体、圆柱体的特性。
- C. 能够独立将三维立体空间问题转化为二维平面问题进行简化计算。

#### 3.6.2. Key terms' definition

face 面 vertex 顶点 vertices 顶点(复数) edge 棱 rectangular solid 长方体 length 长





width 宽 height 高 cube 正方体 volume 体积 surface area 表面积 circular cylinder 圆柱体 lateral surface 侧面(圆柱侧曲面) axis 轴(圆柱中心线) right circular cylinder 直圆柱 sphere / global 球体 cylinder 圆柱 cone 圆锥 prism 棱柱 pyramid 棱锥 dimension 维度

#### 3.6.3 Strategies

圆柱体的体积公式 V=πr<sup>2</sup>h, r 是圆柱体底面的半径, h 是圆柱体的高。777

圆柱体的表面积公式  $S = 2(\pi r^2) + 2\pi rh$ 

其余的立方体表面积公式及体积公式如下图所示:



#### 3.6.4 Exercises

- 1. For the rectangular solid below, find the following.
- (a) Surface area of the solid
- (b) Length of diagonal AB



(b)  $3\sqrt{17}$ 













## 4.1 Graphical Methods for Describing Data

#### 4.1.1 Objectives

- A. 了解基本图形描述变量时所要用到的名词
- B. 了解各种图形表达法,并且可以熟练应用
- C. 了解各种图形的读图方法

#### 4.1.2 Key terms' definition

individual 个体 object 个体 population 群体, 总体

#### variable 变量

• In data analysis, a **variable** is any characteristic that can vary for the population of individuals or objects being analyzed .

#### Distribution of Data 数据分布

• **Distribution of data** indicates the values of the variable and how frequently the values are observed in the data.

#### frequency / count 频数:

• The **frequency**, or **count**, of a particular category or numerical value is the number of times that the category or value appears in the data.

#### frequency distribution 频数分布:

• A **frequency distribution** is a table or graph that presents the categories or numerical values along with their associated frequencies.

#### relative frequency 频率,相对频数:

• The **relative frequency** of a category or a numerical value is the associated frequency divided by the total number of data. Relative frequencies may be expressed in terms of percent, fractions, or decimals.

#### relative frequency distribution 频率分布:

• **Relative Frequency Distribution** (相对频率分布): A **relative frequency distribution** is a table or graph that presents the relative frequencies of the categories or numerical values.

#### **univariate** 单变量的: data observed for one variable.

#### bivariate 双变量的:

• sometimes data are collected to study two different variables in the same population of individuals or objects. Such data are called **bivariate data**.

bar graph / bar chart 柱状图



segmented bar graph 分段柱状图 circle graph / pie chart 饼状图 sector 扇区 histogram 直方图 interval 区间 scatter plot 散点图 trend 趋势 time plot / time series 时间图表

#### 4.1.3 Strategies

#### • Frequency and Relative Frequency:

Example. Here is a list of numbers: 1 3 4 4 4 5 6 7 7 7 7

Here are the resulting frequency and relative frequency distributions of the data.

Number	Frequency (频数)
1	1
3	1
4	3
5	1
6	1
xbF.cn 7新东方在线	4
TOTAL	11

#### Frequency Distribution Table (频数分布表)

在这个例子当中,各个数字发生的次数叫做 **Frequency**(频数);而这样在一组数据中的频数汇总分布,就叫做 **Frequency Distribution**(频数分布)。简略来说,频数分布就是对各个变量频数的特征进行分析。

#### Relative Frequency Distribution Table (相对频数分布表)

Number	Relative Frequency (相对频数)
1	1/11
3	1/11
4	3/11
5	1/11
6	1/11

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	koolearn	4/11	
TOTAL		1	

相对频数=频数/总数,一组数据中相对频数的总和为1。

• Bar Graphs(柱状图):

柱状图适用于离散数据或者分类数据的描述,长方形的 bars 被用来表示数据的种类,所有长方形的宽度 相等,而长度表示的是所代表种类的 frequency 或 relative frequency,每一个长方形间会有固定的举例 做间隔。柱状图可以水平陈列也可以竖直陈列。

柱状图的主要考察点:不同数据的 frequency 或 relative frequency 的比较。



如上图,有的时候柱状图中的长方形还会被分为不同的部分,来表示一个大数据种类下的各个小类别的数据频数或相对频率的分布,这种图形是柱状图的一种,叫做 segmented bar graph 。

• Circle Graphs / pie charts (饼状图):

在饼状图中,一组数据被描述成一个圆形的图形,这组数据中的每一个类别,根据其相对频数占据一定 比列的面积,每一个种类所占的圆的一部分被叫做 sector。

饼图的主要考察点:相对频数计算法。



• Histograms (直方图):

直方图和柱状图很像,但是有两点区别。一,直方图的长方形间是没有固定空隙的;二,直方图的长度和宽度都是有意义的,其宽度代表了该组数据的 interval(区间)。



<sup>•</sup> Scatterplots (散点图):





当描述两个变量关系时,我们可以把一个变量放在横向坐标,而另一个放在纵向坐标,而图像中的点来 表述两个变量的关系。而有时,当两个变量的关系很清晰时,我们可以用一定的趋势线来描述这种 trend (趋势)。



• Time Plots / time series (时间图表)

在时间图表中,横坐标为时间,纵坐标为该时间点上变量的取值。

#### 4.1.4 Exercises



(a) For which year did total expenditures increase the most from the year before?(b) For 2001, private school expenditures were approximately what percent of total expenditures?

Answer: (a) 1998 (b) 19%

2. A bicycle trainer studied 50 bicyclists to examine how the finishing time for a certain bicycle race was related to the amount of physical training in the three months before the race. To measure the amount of training, the trainer developed a training index, measured in "units" and based on the intensity of each bicyclist's training. The data and the trend of the data, represented by a line, are displayed in the scatterplot above.

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(a) How many of the 50 bicyclists had both a training index less than 50 units and a finishing time less than 4.5 hours?

(b) What percent of the 10 fastest bicyclists in the race had a training index less than 90 units?

Answer: (a) 5 (b) 70%

% / Koolean

Questions 3 and 5 are based on the following data.

NUMBER OF OCCUPATIONAL INJURIES IN STATE X, 1998





3. How many of the age-groups each accounted for more than 15 percent of the total number of occupational injuries in State X in 1998?

- A. One
- B. Two
- C. Three
- D. Four
- E. Five

Answer: C

4. In 1998, if one-half of the occupational injuries in the combine 34-and-under age- groups were incurred by men, what was the number of occupational injuries incurred by men in the combined 35-and-over age-groups?

A. 33,500

- B. 31,900
- C. 30,500

D. 25,400 E. 21,700

Answer: D

5. For the 55-64 age-group in 1998, the average (arithmetic mean) number of work- hours lost per occupational injury was 48.5. If a workweek is 40 work-hours, which of the following is closest to the total number of workweeks lost due to occupational injuries in the 55-64 age-group in 1998?

A. 4,500

B. 5,200

C. 5,500

- D. 5,900
- E. 6,300

Answer: E

6.





#### POPULATION OF THE UNITED STATES IN 1800 AND 1900

Year	Population	Population per Square Mile
1800	5.3 million	6.1
1900	76.0 million	25.6

By approximately how many square miles did the area of the United States increase from 1800 to 1900?

$\bigcirc$	360,000
$\bigcirc$	2,000,000
$\bigcirc$	3,625,000
$\bigcirc$	20,000,000
$\bigcirc$	36,250,000

Answer: B

#### Questions 7 and 9 are based on the following data.



7.



For 1988, the typical travel time during the morning commuting hours was approximately what fraction of the typical travel time during the evening commuting hours?

$$\bigcirc \frac{1}{3}$$
$$\bigcirc \frac{2}{5}$$
$$\bigcirc \frac{5}{9}$$
$$\bigcirc \frac{8}{13}$$
$$\bigcirc \frac{2}{3}$$

#### Answer: B 8.



The typical travel time during the morning commuting hours decreased by approximately what percent from 1986 to 1988?	
O 5%	
○ 10%	
○ 25%	
○ 40%	
O 45%	
Answer: C	
9.	

During the morning commuting hours in 1987, what was the average speed, in miles per hour, of a car that traveled the 10 miles on Road H if the car took the typical amount of time to travel the 10 miles?

$\subset$	$\supset$	15
C	>	20
$\subset$	>	25
C	>	33
$\subset$	>	40

Answer: E



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#### 4.2 Numerical Methods for Describing Data

#### 4.2.1 Objectives

A.了解描述数据中心趋势的各项计算方法B.了解描述数据扩散趋势的各项计算方法C.了解箱线图

#### 4.2.2 Key terms' definition

- Central Tendency 中心趋势: Measures of central tendency indicate the "center" of the data along the number line and are usually reported as values that represent the data. There are three common measures of central tendency: (i) the arithmetic mean—usually called the average or simply the mean, (ii) the median, and (iii) the mode.
- Arithmetic Mean 算术平均数: To calculate the mean of *n* numbers, take the sum of the *n* numbers and divide it by *n*.
- Median 中位数 KOOleOn
- Mode 众数
- Weight 权重: The number of times a value appears in the list, or the frequency, is called the weight of that value.
- Weighted Mean 加权平均数: When several values are repeated in a list, it is helpful to think of the mean of the numbers as a weighted mean of only those values in the list that are different. Weighted average=sum (weight\*value)
- Positions O: The three most basic positions, or locations, in a list of data ordered from least to greatest are the beginning, the end, and the middle. It is useful here to label these as *L* for the least, *G* for the greatest, and *M* for the median. Aside from these, the most common measures of position are **quartiles** and **percentiles**.



• Quartiles 四分位数

- Percentiles 百分位数
- Dispersion 扩散: Measures of dispersion indicate the degree of "spread" of the data. The most common

statistics used as measures of dispersion are the range, the interquartile range, and the standard deviation. These statistics measure the spread of the data in different ways.

- Range 极差: The range of the numbers in a group of data is the difference between the greatest number G in the data and the least number L in the data; that is, G L.
- Interquartile Range 四分位差: A measure of dispersion that is not affected by outliers is the interquartile range. It is defined as the difference between the third quartile and the first quartile, that is, *Q Q*.
- standard deviation 标准差: Unlike the range and the interquartile range, the standard deviation is a measure of spread that depends on each number in the list. Using the mean as the center of the data, the standard deviation takes into account how much each value differs from the mean and then takes a type of average of these differences.
- Outlier 异常值
- standardization 标准化
- population standard deviation 总体标准差
- sample standard deviation 样本标准差



4.2.3 Strategies

#### GRE 数学教程





• 基本公示表:

#### • Quartile and Boxplot(四分位数和箱线图)

第一分位数  $Q_1$ ,第二分位数  $Q_2$  (也就是中位数),和第三分位数  $Q_3$ 将一组数据等分为四份。当一组数据 按照递增的方式进行排列的时候,第一组数据包含了从最小值到 $Q_1$ 的所有数据,第二组包括了从 $Q_1$ 到中 位数的所有数据,第三组数据包括了从中位数到  $Q_3$ 的所有数据,而第四组数据包括了从  $Q_3$ 到最大值的 所有数据。因为数组中所包含的数据不一定可以被4整出,在决定 $Q_1$ 和  $Q_3$ 时,不同的统计学家给出了不 同的方法,但是在决定第二分位数时,大家达成了一致:  $Q_2 = M$ 。一般说来,我们采用的方法为:首先 通过 $Q_2 = M$ 的方法,将一组数据一分为二,得到一组较小的数据和一组较大的数据,而将第一分位数 $Q_1$ 取为较小数据组的中位数,第三分位数 $Q_3$ 取为较大数据组的中位数。

**Interquartile Range** (四分位差) 是一个描述数组离散程度的数据,它主要描述一组数据中间半段的离散程 度。它的计算方法为IQR=  $Q_3$ -  $Q_1$ ,也就是说,四分位差不会受outliers(异常值)的影响。

一个描述一组数据中间趋势和离散趋势的方式是描述五个数字L(最小值), $Q_1$ 第一分位数,  $Q_2$ 第二分位数,  $Q_3$ 第三分位数和G最大值。当我们把这五个数字在数轴上标示出来,并在数轴上方画出如下图的图形时,我们就可以得到boxplots or box-and-whisker plots(箱线图)。在箱线图中,"箱子描述的是四分位数,而两端的延伸描述的是最小值和最大值。



#### • Standarization (标准化)

每一个数值都被它所处的数组中的均值和标准差所限制和影响。为了可以比较位于不同均值和标准差的数组的数据,我们可以引入一个概念叫做 standardization (标准化)。在标准化的过程中,述职要减去它所处数组的均值,而这个差值也将继续除以该数据所处数组的标准差。标准化是一个非常有效的工具,因为它为完全不可以直接相比的数据提供了一个比较的途径。



#### 4.2.4 Exercises

1. The numbers of passengers on 9 airline flights were 22, 33, 21, 28, 22, 31, 44, 50, and 19. The standard deviation of these 9 numbers is approximately equal to 10.2.

(a) Find the mean, median, mode, range, and interquartile range of the 9 numbers.

(b) If each flight had had 3 times as many passengers, what would have been the mean, median, mode, range, interquartile range, and standard deviation of the nine numbers?

(c) If each flight had had 2 fewer passengers, what would have been the interquartile range and standard deviation of the nine numbers?

Answer:

(a) mean = 30, median = 28, mode = 22, range = 31, interquartile range = 17 (b) mean = 90, median = 84, mode = 66, range = 93, interquartile range = 51, standard deviation  $\approx 30.7$ 

(c) interquartile range = 17, standard deviation  $\approx 10.2$ 

2. Find the mean and median of the values of the random variable *X*, whose relative frequency distribution is given in the table below.

*X* Relative Frequency



 0	0.18
kooleaín	0.33
新东方在2线	0.10
3	0.06
4	0.33

Answer: mean = 2.03, median = 1

3. Eight hundred insects were weighed, and the resulting measurements, in milligrams, are summarized in the boxplot below.



- (a) What are the range, the three quartiles, and the interquartile range of the measurements?
- (b) If the 80th percentile of the measurements is 130 milligrams, about how many measurements are between 126 milligrams and 130 milligrams?

Answer:

- (a) range=41  $Q_1$ =114  $Q_2$ =118  $Q_3$ =126 IQR=12
- (b) 40 measurements
- 4. x < y-2

Quantity A: The average (arithmetic mean) of x and yQuantity B: y-1

- A. Quantity Ais greater.
- B. Quantity B is greater.
- C. The two quantities are equal
- D. The relationship cannot be determined from the information given.

#### Answer: B

5. In a data set of 10,000 numbers varying from 20 to 80, the number 62 is the 60th percentile and the number 74 is the nth percentile.

Quantity A: *n* Quantity B: 70

- A. Quantity A is greater.
- B. Quantity B is greater.



C. The two quantities are equalD. The relationship cannot be determined from the information given.

Answer: D

6.

Mike, Scott, Jim, Kate, and Pete each have a different number of assignments this month. Pete has fewer assignments than Kate, Kate has more assignments than Mike, Mike has more assignments than Jim, and Jim has more assignments than Scott. Which of the following could be the person who has the median number of assignments this month for the five people listed?

Indicate all such people.

Mike
Scott
Jim
Kate
Pete

Answer:	Mike.	Jim.	Pete

7.

A research report states that the average (arithmetic mean) of 120 measurements was 72.5, the greatest of the 120 measurements was 92.8, and the range of the 120 measurements was 51.6.

The information given above is sufficient to determine the value of which of the following statistics?

Indicate all such statistics.

The least of the 120 measurements

The median of the 120 measurements

The standard deviation of the 120 measurements

The sum of the 120 measurements

Answer:	AD

2	ð





In a certain club, the average (arithmetic mean) age of the 35 males is 24.2 years and the average age of the 25 females is 27.6 years.

Quantity A

Quantity B 25.9

The average age of all of the people in the club

Answer: B

4.3 Counting Methods (计算方法)

#### 4.3.1 Objectives

A. 了解集合问题和维恩图的应用的计算

- B. 了解阶乘、排列组合等计算方法
- C. 了解乘法原则和加法原则

#### 4.3.2 Key terms' definition

set 集合 finite set 有限集合 infinite set 无限集合 empty set 空集 nonempty 非空 element / member 元素 subset 子集 intersection 交集 union 并集 universal set 全集 Venn Diagram 维恩图 disjoint / mutually exclusive 互斥 list 数列 permutation 排列 combination 组合 factorial 阶乘







4.3.3 Strategies kooleon 新东方在线

list 和 set 的区别: list (数列) 里的数字是有顺序的.

#### 集合与维恩图:

 $|A\cup B|{=}|A|{+}|B|{-}|A\cap B|$ 



• Factorial (阶乘):

适用范围: natural numbers (自然数) 表达符号: n! 计算公式: n!=n(n-1)(n-2).....1 特殊公式: 0!=1



• Combination and Permutation (排列组合)





#### • Multiplication Principle and Addition Principle (乘法原则和加法原则)

当完成一件事是可以分步骤完成的,可以通过将每一步的possibilities相乘来计算完成该事件possibilities; 当完成一件事是可以分类完成的,可以通过将每一步的possibilities相加来计算完成该事件possibilities。

#### 4.3.4 Exercises

1. Martha invited 4 friends to go with her to the movies. There are 120 different ways in which they can sit together in a row of 5 seats, one person per seat. In how many of those ways is Martha sitting in the middle seat?

Answer: 24

2. From a box of 10 light bulbs, you are to remove 4. How many different sets of 4 light bulbs could you remove?

Answer: 210

- 3. A talent contest has 8 contestants. Judges must award prizes for first, second, and third places, with no ties.
  - (a) In how many different ways can the judges award the 3 prizes?

kooleoro

(b) How many different groups of 3 people can get prizes?

Answer:

(a) 336 (b) 56

4.4 Probability 概率

#### 4.4.1 Objectives

A. 了解乘法原则和加法原则

B. 了解概率的各项计算

#### 4.4.2 Key terms' definition

possibility 可能性 probability 概率 dice/die 骰子

probability experiment 随机试验:



• A **probability experiment**, also called a **random experiment**, is an experiment for which the result, or outcome, is uncertain. We assume that all of the possible outcomes of an experiment are known before the experiment is performed, but which outcome will actually occur is unknown.

#### sample space 样本空间:

- The set of all possible outcomes of a random experiment is called the sample space.
- event 事件:
- Any particular set of outcomes is called an event. random 随机的

#### random selection 随机抽取:

- The assumption of random selection means that each of the names is equally likely to be selected. **mutually exclusive** 互斥:
- Events that cannot occur at the same time are said to be mutually exclusive.

#### independent 独立:

• E and F are said to be independent if the occurrence of either event does not affect the occurrence of the other.

4.4.3 Strategies

#### • Possibility and Probability (可能性和概率)

在 GRE 考试中,一定要注意区分 Possibility 和 Probability 的区别。这两个单词虽然中文均指可能性,但是 在数学考试中,前者能见到的问法大多是用 How many possibilities does EVENT have?的问句,而后者多见 的是 What is the probability of EVENT?。通过疑问词的区别我们可以看出, possibility 在数学概念中指的是 发生的情况的种类数目,而 probability 指的是概率,是一个介于 0 到 1 (包括边界)的数字,概率越大,

该事件越可能发生。比如,投掷一个六面骰,一共会有 6 possibilities,而投中"1"的 probability  $\mathbb{E}_{6}^{1}$ 。

• Caculation of Probability (概率的计算)

## $P(E) = \frac{\text{the number of outcomes in the event } E}{\text{the number of possible outcomes in the experiment}}$

总体来说,一个event的probability的计算方法为,在一次random experiment中,该事件发生的possibilities和 所有的possibilities之比。

#### 概率遵循如下特征:

- A. 概如果事件A一定发生, P(A) = 1.
- B. 如果事件A一定不发生, P(A)=0.
- C. 如果时间A不一定发不发生,0 < P(A) < 1.



- D. 事件A不发生的概率为 1-P(A).
- E. 如果A为随机事件,那么A发生的概率为所有在A中所发生的结果的概率之和.
- F. 一个随机试验中,所有事件的概率之和为1.
- G. P  $(A \cup B) = P (A) + P (B) P (A \cap B)$
- H. 如果事件A和B mutually exclusive (互斥), P (A∩B) =0, 也就意味着P (A∪B) =P (A) +P (B)
- I. 如果A和B是independent(独立)的,那么P(A∩B)=P(A)P(B),也就意味着P(A∪B)=P(A)+P
   (B) P(A)P(B)

#### 4.4.4 Exercises

1. If an integer is randomly selected from all positive 2-digit integers, what is the probability that the integer chosen has

- a) a 4 in the tens place?
- b) at least one 4 in the tens place or the units place?
- c) no 4 in either place?

#### Answer:

(a) 1/9

(b) 1/5

(c) 4/5

2. In a box of 10 electrical parts, 2 are defective.

- a) If you choose one part at random from the box, what is the probability that it is not defective?
- b) If you choose two parts at random from the box, without replacement, what is the probability that both are defective?

Answer:

(a) 4/5

(b) 1/45

3. The table shows the distribution of a group of 40 college students by gender and class.

	Sophomores	Juniors	Seniors
Males	6	10	2
Females	10	9	3

If one student is randomly selected from this group, find the probability that the student chosen is

- a) not a junior
- b) a female or a sophomore



c) a male sophomore or a female senior
Answer:
(a) 21/40
(b) 7/10
(c) 9/40

4. Let A,B,C, and D be events for which P(A or B)=0.6, P(A)=0.2, P(C or D)=0.6, and P(C)=0.5. The events A and B are mutually exclusive, and the events C and D are independent.

a) Find P(B)

b) Find P(D)

Answer:

(a) 0.4

(b) 0.2

5. Lin and Mark each attempt independently to decode a message. If the probability that Lin will decode the message is 0.80 and the probability that Mark will decode the message is 0.70, find the probability that

- a) both will decode the message
- b) at least one of them will decode the message



c) neither of them will decode the message

Answer:

- (a) 0.56
- (b) 0.94
- (c) 0.06



If an integer greater than 100 and less than 1,000 is to be selected at random, what is the probability that the integer selected will be a multiple of 7?

0	<u>142</u> 999
0	<u>142</u> 900
0	<u>142</u> 899
0	<u>128</u> 900
0	128

#### Answer: E

64



#### 4.5 Distributions of Data, Random Variables, and Probability Distributions 数据、随机变量和概率的分布

#### 4.5.1 Objectives

- A. 了解各类分布的特征
- B. 了解正态分布和标准正态分布的各项指标的计算方法
- C. 熟练掌握 Z-score 的标准化计算

#### 4.5.2 Key terms' definition

#### random variable 随机变量:

• In data analysis, variables whose values depend on chance play an important role in linking distributions of data to probability distributions. Such variables are called random variables.

#### distribution curve 分布曲线:

• The distribution can be modeled by a smooth curve that is close to the tops of the bars in the bar charts or histograms, and if the vertical scale can be adjusted (stretched or shrunk) so that the sum of the areas of the bars is 1. With this vertical scale adjustment, the area under the curve that models the distribution is also 1. This model curve is called a distribution curve, but it has other names as well, including density curve and frequency curve.

#### discrete random variable 离散随机变量:

• The variables that their values consist of discrete points on a number line.

#### uniform distribution 均匀分布: \_\_\_\_\_

- The probability is distributed uniformly over all possible outcomes. **normal distribution** 正态分布:
- Many natural processes yield data that have a relative frequency distribution shaped somewhat like a bell, as in the distribution below with mean *m* and standard deviation *d*.

#### continuous random variable 连续随机变量:

• The area of the region under the curve is 1, and the areas of vertical slices of the region—similar to the bars of a histogram—are equal to probabilities of a random variable associated with the distribution. Such a random variable is called a continuous random variable.

#### standard normal distribution 标准正态分布:

• The standard normal distribution is a normal distribution with a mean of 0 and standard deviation equal to 1. **expected value 期望** 





# 4.5.3 Strategies kooleon

#### • Distribution of Data (数据分布)

- A.分布曲线的作用在于,抛开数据的分类不看,通过观察曲线,该组数据大体的分布趋势可以被直观地 观测到。随意确定一个横轴上的区间,这个区间内所对应的去线下的面积代表着,在该组数据内,数 据位于该区间的概率。
- B.为了更精确地表达出数据的分布,在分布曲线的横轴上均值(m)和中位数(M)以及标准差(d)会 被表达出来。并且有多少数据回落在 m±3d 这个区间内一般被认为是衡量一组数据是否集中地判断标 准之一。
- C.中位数(M)根据其定义会将一组数据分为小的部分和大的部分两个等份。而均值(m)则是将所有数据都纳入计量后得出的中间水平,所以可能大于也可能小于中位数。如果 m 大于 M,我们认为这组数据有一些极大的数字;反之,我们认为这组数据有一些极小的数字。
- data 所对应的 relative frequency 和 variable 所对应的 probability 是一件事,因此 variable 也会有其对应 的图像,并且有均值和中位数。
- Expected value (期望): Variable X的均值可以被称为mean of the random variable X,也可以称为 expected value,记做E(X)。期望为离散型随机变量的一切可能的取值xi与对应的概率pi乘积之和.

$$E(X) = \sum_{i=1}^{n} x_i \cdot p_i$$

#### • Normal Distribution (正态分布)

A. 正态分布的均值、中位数和众数是近乎相同的

- B. 68-95-99.7法则:在正态分布中,有68%的数据落入m±d的区间内,有95%的数据落入m±2d的区间内, 有99.7%的数据落入m±3d的区间内
- C. 一组变量的均值决定了正态分布的中心位置,而标准差决定了他的陡峭程度
- D. 正态分布适用于连续变量,而在连续变量中,取到具体一个值的概率为0
- E. 正态分布线下的面积为1,任意横轴区间内所对应的线下面积,为变量的值取到该区间内的概率





#### • Standard Normal Distribution (标准正态分布)

标准正态分布指均值为0,标准差为1的正态分布,任何正态分布都可以通过对其变量进行standardization(标 准化)的变换而转换到标准正态分布。

#### 4.5.4 Exercises

1.



The figure shows a normal distribution with mean m and standard deviation d, including approximate percents of the distribution corresponding to the six regions shown.

Suppose the heights of a population of 3,000 adult penguins are approximately normally distributed with a mean of 65 centimeters and a standard deviation of 5 centimeters.

- (a) Approximately how many of the adult penguins are between 65 centimeters and 75 centimeters tall?
- (b) If an adult penguin is chosen at random from the population, approximately what is the probability that the penguin's height will be less than 60 centimeters? Give your answer to the nearest 0.05.

Answer: (a) 1440 (b) 0.15

2.



Ħ

In a distribution of the values of the variable x, the 50th percentile is 48.5 and the 60th percentile is 56.5.

Quantity A

Quantity B

40.5

The 40th percentile of the distribution of the values of x

Answer: D







Appendix 常见英文单位表达与换算 (1) 金钱单位 cent 一美分(硬币) penny 一美分(硬币) nickle 五美分(硬币) dime 十美分/角(硬币) quarter 二十五美分(硬币) dollar 美元 (2) 数量单位 half 一半, 二分之一 quarter 四分之一 dozen 打 (12个) score 廿 (20个) (3) 温度单位 Centigrade 摄氏 Fahrenheit 华氏 F = C \* 1.8 + 32(4) 体积单位 liter 升 1 milliliter 毫升 ml gallon 加仑 gal quart 夸脱 qt pint 品脱 pt (干量或液量的单位) gill 及耳 gi ounce 盎司 oz (小额重量单位,液体,贵金属) (5) 长度单位 三 C N 利力 / 71 土 2 支 meter 米 m kilometer 千米 km decimeter 分米 dm centimeter 厘米 cm millimeter 毫米 mm inch (复数 inches) 英寸 in foot (复数 feet) 英尺 ft yard 码 yd mile 英里 mi <u>1 ft = 12 in</u> <u>1 yd=3 ft</u> 1 mi = 1760 yd(6) 质量单位 gram 克 g kilogram 千克 kg ton 吨 t





pound 磅 lb ounce 盎司 oz <u>1 pound = 0.454 kg</u>











Vocabulary

abscissa 横坐标 absolute value 绝对值 acute angle锐角 add 加 adjacent angle 邻角 algebraic term 代数项 alternate interior angle 内错角 angles 角 arc 弧 area 面积 arithmetic mean 算术平均数 axis 轴 (圆柱中心线) bar chart 柱状图 bar graph 柱状图 base 底 base 底数 bisect 平分 bisector平分线 bivariate 双变量的 cent 一美分(硬币) center 圆心 Centigrade摄氏 centimeter 厘米 cm central angle 圆心角 central tendency 中心趋势 chord 弦 circle graph 饼状图 circle 圆 circular cylinder 圆柱体 circumference 圆的周长 circumscribe 外接 / 外切 combination 组合 common denominator 公分母 complementary angle 余角 complementary 互余 composite number 合数 compound interest 复利 concentric circles 同心圆 conduct 实施 cone 圆锥 congruent angles 等角



congruent line segments 全等线段 congruent triangle 全等三角形 新东方在线 consecutive number 连续数 constant 常数 continuous random variable 连续随机变量 coordinate system 坐标系 Corresponding angle 同位角 count 频数 cube root 立方根 cube 正方体 cylinder 圆柱 decagon 十边形 decimal 小数 decimeter 分米 dm denominator 分母 diagonal对角线 diagram 图 diameter 直径 dice 骰子 die 骰子 difference 差 digit 数位 dime 十美分/角(硬币) dimension 维度 directly proportional to 正比于 discount 折扣 discrete random variable 离散随机变量 disjoint 互斥 dispersion 扩散 distinct 不同的 distribution curve 分布曲线 distribution of data 数据分布 divide 除 divisible 可被整除的 divisor 因数 dollar 美元 domain 定义域 dozen 打 (12个) edge 棱 element 元素 elimination: 消元法 empty set 空集 endpoint 端点 equation 等式, 方程

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equilateral triangle 等边三角形 equivalent equations 等价方程式 even integer 偶数 event 事件 expected value 期望 exponent 指数 exterior angle 外角 externally tangent 外切 face 面 factor 因数 factorial 阶乘 factoring 因式分解 Fahrenheit 华氏 feet 英寸 (复数) Figure not drawn to scale 图形不按比例绘制 finite set 有限集合 foot 英尺 ft formula 公式 fourth root 四次方根 fraction 分数 frequency distribution 频数分布 frequency 频数 function 函数 gallon 加仑 gal gill 及耳 gi global 球体 gram 克 g greater than or equal to 大于等于 greater than 大于 greatest common divisor 最大公因数 greatest common factor 最大公因数 half 一半, 二分之一 height 高 hexagon 六边形 histogram 直方图 hundreds digit 百位 hundredths digit 百分位 hypotenuse 斜边 identity 恒等式 improper fraction 假分数 inch 英寸 in inches 英寸(复数) inclusive 包含的 independent 独立







individual 个体 Inequalities 不等式 infinite set 无限集合 inscribe 内接 / 内切 integer 整数 intercept 截距 interest rate 利率 interest 利息 interior angle 内角 interior angles on the same side 同旁内角 internally tangent 内切 interquartile range 四分位差 intersect 相交 intersection 交集 interval 区间 inversely proportional to 反比于 irrational number 无理数 isosceles triangle 等腰三角形 kilogram 千克 kg kilometer 千米 km lateral surface 侧面(圆柱侧曲面) least common multiple 最小公倍数 leg 直角边 length 长 length 长度 less than or equal to 小于等于 less than 小于 like terms 同类项 line of symmetry 对称轴 line segment 线段 linear equation 线性方程 lines 直线 list price 标价 list 数列 liter 升 1 literal coefficient 字母系数 margin 利润 mark down 降价 mark up 涨价 mean median 中位数 member 元素 meter 米 m midpoint 中点







mile 英里 mi milliliter 毫升 ml millimeter 毫米 mm minus 减 mixed number 带分数 mode 众数 more than 大于 multiple 倍数 multiply 乘 mutually exclusive 互斥 negative number 负数 nickel 五美分(硬币) nonempty 非空 normal distribution 正态分布 number line数轴 numerator 分子 numerical coefficient 数字系数 object 个体 obtuse angle钝角 octagon 八边形 odd integer 奇数 ones digit 个位 opposite angles 对顶角 ordinate 纵坐标 origin 原点 original price 原价 ounce 盎司 oz (小额重量单位,液体,贵金属) outlier 异常值 parabola 抛物线 parallel 平行 parallelogram 平行四边形 penny 一美分(硬币) pentagon 五边形 percent change 百分比变化 percent decrease 百分比减 percent increase 百分比增 percent 百分比 percentiles 百分位数 perimeter 周长 permutation 排列 perpendicular 垂直 pie chart 饼状图 piecewise-defined function 分段函数 pint 品脱 pt (干量或液量的单位)





plus 加 point of tangency 切点 polygon 多边形 population standard deviation 总体标准差 population 群体, 总体 positions 位置 positive number 正数 possibility 可能性 pound 磅 lb power 次方,幂 prime divisor 质因数 prime factor 质因数 prime number 质数 principal 资本 prism 棱柱 probability experiment 随机试验 probability 概率 product 积 profit 利润 proportion 比例 proportional to 正比于 purchasing price 买价 pyramid 棱锥 Pythagorean theorem勾股定理 quadrant 象限 quadratic equation 二次方程 quadrilateral 四边形 quadruple 四倍 quantity 数量 quart 夸脱 qt quarter 二十五美分(硬币) quarter 四分之一 quartiles 四分位数 questionnaire 问卷 quotient 商 radian弧度 radii 半径 (复数) radius 半径 random experiment 随机试验 random selection 随机抽取 random variable 随机变量 random 随机的 range 值域 range 极差



新 Kooleo 新 东 方 街 新 东 方 街





rate 率 ratio 比例 rational numbers 有理数 ray 射线 real number line 实数轴 real number 实数 reciprocal 倒数 rectangle 长方形 rectangular coordinate system 直角坐标系 rectangular solid 长方体 regular polygon 正多边形 relative frequency distribution 频率分布 relative frequency 频率,相对频数 remainder 余数 repeat decimal 循环小数 retail value 零售价 rhomb 菱形 right angle 直角 right circular cylinder 直圆柱 right triangles 直角三角形 round to the nearest 四舍五入 sale price 卖价 sales tax 消费税 sample space 样本空间 sample standard deviation 样本标准差 scatter plot 散点图 score 廿 (20个) sector 扇区 sector 扇形 segmented bar graph 分段柱状图 semicircle半圆 set 集合 side 边, 边长 similar terms 同类项 similar triangles 相似三角形 simultaneous equations 联立方程 single interest 单利 slope 斜率 solution set 解集 sphere 球体 square root 平方根 square 平方 square 正方形 standard deviation 标准差





standard normal distribution 标准正态分布 standardization 标准化 subset 子集 substitution: 连立法 subtract 减 sum 和 supplementary angle 补角 supplementary 互补 surface area 表面积 survey 调查 symmetric 对称 system of equations 方程组 tangent line 切线 tangent 相切 tax 税 tens digit 十位 tenths digit 十分位 terminate decimal 有限小数 thousands digit 千位 thousandths digit 千分位 time plot 时间图表 time series 时间图表 time 乘 ton 吨 t trapezoid 梯形 trend 趋势 triangle 三角形 triple 三倍 twice 两倍 undefined 不可定义的 uniform distribution 均匀分布 union 并集 units digit 个位 univariate 单变量的 universal set 全集 variable 变量 Venn Diagram 维恩图 vertex 顶点 vertex 交点 vertical angles 对顶角 vertices 顶点(复数) vertices 交点(复数) volume 体积 weighted mean 加权平均数

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weight权重 width 宽 x-axis x轴



x-coordinate 横坐标 xy-coordinate system 平面直角坐标系 xy-plane 平面直角坐标系 yard 码 yd y-axis y轴 y-coordinate 纵坐标



